## Modeling Forum

# Results of the 1995 Mathematical Contest in Modeling 

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## Introduction

A total of 320 teams of undergraduates, from 194 schools, spent the third weekend in February working on applied mathematics problems. They were part of the eleventh Mathematical Contest in Modeling (MCM). On Friday morning, the MCM faculty advisor opened a packet and presented each team of three students with a choice of one of two problems. After a weekend of hard work, typed solution papers were mailed to COMAP on Monday. Seven of the top papers appear in this issue of The UMAP Journal.

Results and winning papers from the first ten contests were published in special issues of Mathematical Modeling (1985-1987) and The UMAP Journal (1985-1994). The 1994 volume of Tools for Teaching, commemorating the tenth anniversary of the contest, contains all of the 20 problems used in the first ten years of the contest and a winning paper for each. Limited quantities of that volume and of the special MCM issues of the Journal for the last few years are available from COMAP.

## Problem A: The Single Helix

The problem consists of assisting a small biotechnological company in designing, proving, programming, and testing a mathematical algorithm to locate "in real time" all the intersections of a helix and a plane in general positions in space (see Figure 1).

Similar programs for Computer Aided Geometric Design (CAGD) enable engineers to view a plane section of the object that they design, for example, an aircraft jet engine, an automobile suspension, or a medical device. Moreover, engineers may also display on the plane section such quantities as air flow, stress, or temperature, coded by colors or level curves. Furthermore,


Figure 1. Some intersections of a helix with a plane.
engineers may rapidly sweep such plane sections through the entire object to gain a three-dimensional visualization of the object and its reactions to motion, forces, or heat. To achieve such results, the computer programs must locate all the intersections of the viewed plane and every part of the designed object with sufficient speed and accuracy. General "equation solvers" may in principle compute such intersections; but for specific problems, special methods may prove faster and more accurate than general methods. In particular, general software for Computer Aided Geometric Design may prove too slow to complete computations in real time, or too large to fit in the finished medical devices being developed by the company. The considerations just explained have led the company to the following problem.

Problem: Design, justify, program, and test a method to compute all the intersections of a plane and a helix in general positions (at any locations and with any orientations) in space.

A segment of the helix may represent, for example, a helicoidal suspension spring or a piece of tubing in a chemical or medical apparatus.

The need for some theoretical justification of the proposed algorithm arises from the necessity of verifying the solution from several points of view. This can be done through mathematical proofs of parts of the algorithm, and through tests of the final program with known examples. Such documentation and tests will be required by government agencies for medical use.

## Problem B: Aluacha Balaclava College

Aluacha Balaclava College has just hired a new Provost. Problems with faculty compensation at the college forced the former Provost to resign, so the new Provost needs to make the institution of a fair and reasonable compensation system her first priority. As a first step in this process, she has hired your team as consultants to design a compensation system that reflects the following circumstances and principles.

## Circumstances

There are four faculty ranks: Instructor, Assistant Professor, Associate Professor and Professor, in ascending order. Faculty with Ph.D. degrees are hired at the rank of Assistant Professor. Faculty who are working on a Ph.D. are hired at the rank of Instructor and promoted automatically to Assistant Professor upon completion of their degrees. Faculty may apply for promotion from Associate Professor to Professor after serving at the rank of Associate for seven or more years. The promotion decisions are made by the Provost with recommendations from a faculty committee and are not your concern.

Faculty salaries are for the ten-month period September through June. Raises are always effective beginning in September. The total amount of money available for raises varies from year to year and generally is not known until March for the following year.

The starting salary this year for an Instructor with no prior teaching experience was $\$ 27,000$ and for an Assistant Professor was $\$ 32,000$. Faculty can receive credit, upon hire, for as much as seven years of teaching experience at other institutions.

## Principles

- All faculty should get a raise any year that money is available.
- Faculty should get a substantial benefit from promotion. If one is promoted in the minimum possible time, the benefit should be roughly equal to seven years of normal (non-promotion) raises.
- Faculty who get promoted on time (after seven or eight years in rank) and have careers of 25 or more years should make roughly twice as much at retirement as a new Ph.D. starting off.
- Faculty in the same rank with more experience should be paid more than others with less experience. But the effect of an additional year of experience should diminish over time. In other words, if two faculty stay in the same rank, their salaries should tend to get closer over time.


## The Project

First, design a new pay system without cost-of-living increases. Then incorporate cost-of-living increases. The final piece of this project is to design a transition process for existing faculty that will move all salaries towards your system without cutting anyone's salary. The existing faculty salaries, ranks and years of service, are in Table 1. Discuss any refinements that you think would improve your system.

The Provost has asked for a detailed pay system plan that she can use for implementation, as well as a short executive summary in clear language, which she can present to the Board and to the faculty. The summary should outline the model, its assumptions, its strengths and weaknesses, and the expected results.

## The Results

The solution papers were coded at COMAP headquarters so that names and affiliations of the authors would be unknown to the judges. Each paper was then read preliminarily by two "triage" judges at Salisbury State University, Maryland. At the triage stage, the summary and overall organization are the basis for judging a paper. If the judges' scores diverged for a paper, the judges conferred; if they still did not agree on a score, a third judge evaluated the paper.

Final judging took place at Harvey Mudd College, Claremont, California. The judges classified the papers as follows:

|  |  |  |  |  | Honorable <br> Mention |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Outstanding | Sarticipation |  |  |  |  | Total

The judges designated seven papers as Outstanding. They appear in this special issue of The UMAP Journal. We list those teams and the Meritorious teams (and advisors) below; the list of all participating schools, advisors, and results is in the Appendix.

Table 1.
Salary data for Problem B.

| Case | Years | Rank | Salary | Case | Years | Rank | Salary | Case | Years | Rank | Salary |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 4 | ASSO | 54,000 | 2 | 19 | ASST | 43,508 | 3 | 20 | ASST | 39,072 |
| 4 | 11 | PROF | 53,900 | 5 | 15 | PROF | 44,206 | 6 | 17 | ASST | 37,538 |
| 7 | 23 | PROF | 48,844 | 8 | 10 | ASST | 32,841 | 9 | 7 | ASSO | 49,981 |
| 10 | 20 | ASSO | 42,549 | 11 | 18 | ASSO | 42,649 | 12 | 19 | PROF | 60,087 |
| 13 | 15 | ASSO | 38,002 | 14 | 4 | ASST | 30,000 | 15 | 34 | PROF | 60,576 |
| 16 | 28 | ASST | 44,562 | 17 | 9 | ASST | 30,893 | 18 | 22 | ASSO | 46,351 |
| 19 | 21 | ASSO | 50,979 | 20 | 20 | ASST | 48,000 | 21 | 4 | ASST | 32,500 |
| 22 | 14 | ASSO | 38,462 | 23 | 23 | PROF | 53,500 | 24 | 21 | ASSO | 42,488 |
| 25 | 20 | ASSO | 43,892 | 26 | 5 | ASST | 35,330 | 27 | 19 | ASSO | 41,147 |
| 28 | 15 | ASST | 34,040 | 29 | 18 | PROF | 48,944 | 30 | 7 | ASST | 30,128 |
| 31 | 5 | ASST | 35,330 | 32 | 6 | ASSO | 35,942 | 33 | 8 | PROF | 57,295 |
| 34 | 10 | ASST | 36,991 | 35 | 23 | PROF | 60,576 | 36 | 20 | ASSO | 48,926 |
| 37 | 9 | PROF | 57,956 | 38 | 32 | ASSO | 52,214 | 39 | 15 | ASST | 39,259 |
| 40 | 22 | ASSO | 43,672 | 41 | 6 | INST | 45,500 | 42 | 5 | ASSO | 52,262 |
| 43 | 5 | ASSO | 57,170 | 44 | 16 | ASST | 36,958 | 45 | 23 | ASST | 37,538 |
| 46 | 9 | PROF | 58,974 | 47 | 8 | PROF | 49,971 | 48 | 23 | PROF | 62,742 |
| 49 | 39 | ASSO | 52,058 | 50 | 4 | INST | 26,500 | 51 | 5 | ASST | 33,130 |
| 52 | 46 | PROF | 59,749 | 53 | 4 | ASSO | 37,954 | 54 | 19 | PROF | 45,833 |
| 55 | 6 | ASSO | 35,270 | 56 | 6 | ASSO | 43,037 | 57 | 20 | PROF | 59,755 |
| 58 | 21 | PROF | 57,797 | 59 | 4 | ASSO | 53,500 | 60 | 6 | ASST | 32,319 |
| 61 | 17 | ASST | 35,668 | 62 | 20 | PROF | 59,333 | 63 | 4 | ASST | 30,500 |
| 64 | 16 | ASSO | 41,352 | 65 | 15 | PROF | 43,264 | 66 | 20 | PROF | 50,935 |
| 67 | 6 | ASST | 45,365 | 68 | 6 | ASSO | 35,941 | 69 | 6 | ASST | 49,134 |
| 70 | 4 | ASST | 29,500 | 71 | 4 | ASST | 30,186 | 72 | 7 | ASST | 32,400 |
| 73 | 12 | ASSO | 44,501 | 74 | 2 | ASST | 31,900 | 75 | 1 | ASSO | 62,500 |
| 76 | 1 | ASST | 34,500 | 77 | 16 | ASSO | 40,637 | 78 | 4 | ASSO | 35,500 |
| 79 | 21 | PROF | 50,521 | 80 | 12 | ASST | 35,158 | 81 | 4 | INST | 28,500 |
| 82 | 16 | PROF | 46,930 | 83 | 24 | PROF | 55,811 | 84 | 6 | ASST | 30,128 |
| 85 | 16 | PROF | 46,090 | 86 | 5 | ASST | 28,570 | 87 | 19 | PROF | 44,612 |
| 88 | 17 | ASST | 36,313 | 89 | 6 | ASST | 33,479 | 90 | 14 | ASSO | 38,624 |
| 91 | 5 | ASST | 32,210 | 92 | 9 | ASSO | 48,500 | 93 | 4 | ASST | 35,150 |
| 94 | 25 | PROF | 50,583 | 95 | 23 | PROF | 60,800 | 96 | 17 | ASST | 38,464 |
| 97 | 4 | ASST | 39,500 | 98 | 3 | ASST | 52,000 | 99 | 24 | PROF | 56,922 |
| 100 | 2 | PROF | 78,500 | 101 | 20 | PROF | 52,345 | 102 | 9 | ASST | 35,798 |
| 103 | 24 | ASST | 43,925 | 104 | 6 | ASSO | 35,270 | 105 | 14 | PROF | 49,472 |
| 106 | 19 | ASSO | 42,215 | 107 | 12 | ASST | 40,427 | 108 | 10 | ASST | 37,021 |
| 109 | 18 | ASSO | 44,166 | 110 | 21 | ASSO | 46,157 | 111 | 8 | ASST | 32,500 |
| 112 | 19 | ASSO | 40,785 | 113 | 10 | ASSO | 38,698 | 114 | 5 | ASST | 31,170 |
| 115 | 1 | INST | 26,161 | 116 | 22 | PROF | 47,974 | 117 | 10 | ASSO | 37,793 |
| 118 | 7 | ASST | 38,117 | 119 | 26 | PROF | 62,370 | 120 | 20 | ASSO | 51,991 |
| 121 | 1 | ASST | 31,500 | 122 | 8 | ASSO | 35,941 | 123 | 14 | ASSO | 39,294 |
| 124 | 23 | ASSO | 51,991 | 125 | 1 | ASST | 30,000 | 126 | 15 | ASST | 34,638 |
| 127 | 20 | ASSO | 56,836 | 128 | 6 | INST | 35,451 | 129 | 10 | ASST | 32,756 |
| 130 | 14 | ASST | 32,922 | 131 | 12 | ASSO | 36,451 | 132 | 1 | ASST | 30,000 |
| 133 | 17 | PROF | 48,134 | 134 | 6 | ASST | 40,436 | 135 | 2 | ASSO | 54,500 |
| 136 | 4 | ASSO | 55,000 | 137 | 5 | ASST | 32,210 | 138 | 21 | ASSO | 43,160 |
| 139 | 2 | ASST | 32,000 | 140 | 7 | ASST | 36,300 | 141 | 9 | ASSO | 38,624 |
| 142 | 21 | PROF | 49,687 | 143 | 22 | PROF | 49,972 | 144 | 7 | ASSO | 46,155 |
| 145 | 12 | ASST | 37,159 | 146 | 9 | ASST | 32,500 | 147 | 3 | ASST | 31,500 |
| 148 | 13 | INST | 31,276 | 149 | 6 | ASST | 33,378 | 150 | 19 | PROF | 45,780 |
| 151 | 4 | PROF | 70,500 | 152 | 27 | PROF | 59,327 | 153 | 9 | ASSO | 37,954 |
| 154 | 5 | ASSO | 36,612 | 155 | 2 | ASST | 29,500 | 156 | 3 | PROF | 66,500 |
| 157 | 17 | ASST | 36,378 | 158 | 5 | ASSO | 46,770 | 159 | 22 | ASST | 42,772 |
| 160 | 6 | ASST | 31,160 | 161 | 17 | ASST | 39,072 | 162 | 20 | ASST | 42,970 |
| 163 | 2 | PROF | 85,500 | 164 | 20 | ASST | 49,302 | 165 | 21 | ASSO | 43,054 |
| 166 | 21 | PROF | 49,948 | 167 | 5 | PROF | 50,810 | 168 | 19 | ASSO | 51,378 |
| 169 | 18 | ASSO | 41,267 | 170 | 18 | ASST | 42,176 | 171 | 23 | PROF | 51,571 |
| 172 | 12 | PROF | 46,500 | 173 | 6 | ASST | 35,798 | 174 | 7 | ASST | 42,256 |
| 175 | 23 | ASSO | 46,351 | 176 | 22 | PROF | 48,280 | 177 | 3 | ASST | 55,500 |
| 178 | 15 | ASSO | 39,265 | 179 | 4 | ASST | 29,500 | 180 | 21 | ASSO | 48,359 |
| 181 | 23 | PROF | 48,844 | 182 | 1 | ASST | 31,000 | 183 | 6 | ASST | 32,923 |
| 184 | 2 | INST | 27,700 | 185 | 16 | PROF | 40,748 | 186 | 24 | ASSO | 44,715 |
| 187 | 9 | ASSO | 37,389 | 188 | 28 | PROF | 51,064 | 189 | 19 | INST | 34,265 |
| 190 | 22 | PROF | 49,756 | 191 | 19 | ASST | 36,958 | 192 | 16 | ASST | 34,550 |
| 193 | 22 | PROF | 50,576 | 194 | 5 | ASST | 32,210 | 195 | 2 | ASST | 28,500 |
| 196 | 12 | ASSO | 41,178 | 197 | 22 | PROF | 53,836 | 198 | 19 | ASSO | 43,519 |
| 199 | 4 | ASST | 32,000 | 200 | 18 | ASSO | 40,089 | 201 | 23 | PROF | 52,403 |
| 202 | 21 | PROF | 59,234 | 203 | 22 | PROF | 51,898 | 204 | 26 | ASSO | 47,047 |

## Outstanding Teams

## Institution and Advisor

## Helix Intersections Papers

"A Specialized Root-Finding Method for Rapidly Determining the Intersections of a Plane and a Helix"
Harvey Mudd College
Claremont, CA
David L. Bosley
"The Single Helix"
Iowa State University
Ames, IA
Stephen J. Willson
"Planes and Helices"
Macalester College
St. Paul, MN
A. Wayne Roberts

Matthew Evans
Andrew Flint
Noah Kubow
R. Robert Hentzel

Scott Williams

Samar Lotia
Eric Musser
Simeon Simeonov

## Faculty Salaries Papers

"Paying Professors What They're Worth"
Harvey Mudd College
Claremont, CA
David L. Bosley
"The World's Most Complicated Payroll"
North Carolina School of Science \& Mathematics
Durham, NC
Dot Doyle
"Long-Term and Transient Pay Scale for College Faculty"
Southeast Missouri State University
Cape Girardeau, MO
Robert W. Sheets
"How to Keep Your Job as Provost"
University of Alaska Fairbanks
Fairbanks, AK
John P. Lambert

Jay Rosenberger
Andrew M. Ross
Dan Snyder

Frank Thorne
W. Garrett Mitchener

Marci Gambrell

Christena Byerley
Christina Phillips
Cliff Sodergren

Liam Forbes
Marcus Martin
Michael Schmahl

## Meritorious Teams

Helix Intersections Papers (13 teams)<br>Baylor University, Waco, TX (Frank H. Mathis)<br>Beijing Institute of Tech., Beijing, China (Yan-ping Zhao)<br>California Polytechnic State Univ., San Luis Obispo, CA (Thomas O'Neil) (two teams)<br>Duke University, Durham, NC (David P. Kraines)<br>Harvard University, Cambridge, MA (Harry R. Lewis)<br>Lewis \& Clark College, Portland, OR (Robert W. Owens)<br>Natl. Univ. of Defense Tech., Changsha, Hunan, China (Wang XiaoXing)<br>New Mexico Inst. of Mining and Tech., Socorro, NM (Brian T. Borchers)<br>South China University of Tech., Guangzhou, Canton, China (Lejun Xie)<br>Southeast University, Nanjing, Jiangsu, China (Huangjun Sunzhizhong)<br>Trinity College Dublin, Dublin, Ireland (Timothy G. Murphy)<br>University College Galway, Galway, Ireland (M. Tuite)<br>University of Alaska Anchorage, Anchorage, AK (Ted L. Gifford)<br>University of Utah, Salt Lake City, UT (Don H. Tucker)<br>Worcester Polytechnic Institute, Worcester, MA (Arthur C. Heinricher)<br>Xidian University, Xian, Shaanxi, China (Wang Yu Ping)<br>Xidian University, Xian, Shaanxi, China (Ma Yu Xiang)<br>Faculty Salaries Papers (26 teams)<br>College of William \& Mary, Williamsburg, VA (Hugo J. Woerdeman)<br>Fudan University, Shanghai, China (Cao Yuan)<br>Fudan University, Shanghai, China (Tan Yongji)<br>Harbin Institute of Technology, Harbin, China (Shi Peilin)<br>Hiram College, Hiram, OH (James R. Case)<br>JiLin University, Changchun, Jilin, China (Lu Xian Yui)<br>Kenyon College, Gambier, OH (Dana N. MacKenzie)<br>Luther College, Decorah, IA (Reginald D. Laursen)<br>Mt. St. Mary's College, Emmitsburg, MD (Fred J. Portier)<br>Muhlenberg College, Allentown, PA (David A. Nelson)<br>Natl. Univ. of Defense Tech., Changsha, Hunan, China (Wu MengDa)<br>Shanghai Jiatong University, Shanghai, China (Longwan Xiang)<br>Southwestern University, Georgetown, TX (Therese Shelton)<br>Texas A \& M Univ., College Station, TX (Denise E. Kirschner)<br>Trinity College Dublin, Dublin, Ireland (James C. Sexton)<br>U.S. Air Force Academy, USAF Academy, CO (Jeffrey S. Stonebraker)<br>Univ. of Alaska Fairbanks, Fairbanks, AK (Patricia A. Andresen)<br>Univ. of Colorado at Denver, Denver, CO (David C. Fisher)<br>Univ. of Missouri-Rolla, Rolla, MO (Roger H. Hering)<br>University of Dallas, Irving, TX (Charles A. Coppin)<br>University of Dayton, Dayton, OH (Ralph C. Steinlage)<br>Vilnius University, Vilnius, Lithuania (Ricardas Kudzma)<br>Wake Forest University, Winston-Salem, NC (Stephen B. Robinson)<br>Washington University, St. Louis, MO (Hiro Mukai)<br>Wheaton College, Wheaton, IL (Paul Isihara)<br>Xidian University, Xian, Shaanxi, China (Mao Yong Cai)

## Awards and Contributions

Each participating MCM advisor and team member received a certificate signed by the Contest Director and the appropriate Head Judge.

The Institute for Operations Research and the Management Sciences (INFORMS) awarded to each member of two Outstanding teams a cash award and a three-year membership. The teams were from Macalester College (Helix Intersections Problem) and Harvey Mudd College (Faculty Salaries Problem). The teams made presentations at a special MCM session and were given cash awards. Moreover, INFORMS gave free one-year memberships to all members of Meritorious and Honorable Mention teams.

The Society for Industrial and Applied Mathematics (SIAM) designated one Outstanding team from each problem as a SIAM Winner. Each team member received a cash prize, and each team received a subsidized trip to the July 1995 SIAM Annual Meeting in San Diego, CA. The teams were from Iowa State University (Helix Intersections Problem) and from University of Alaska Fairbanks (Faculty Salaries Problem). These teams made presentations at a special modeling minisymposium.

## Judging

## Director

Frank R. Giordano, Dept. of Mathematical Sciences, U.S. Military Academy, West Point, NY

## Associate Directors

Chris Arney, Dept. of Mathematical Sciences, U.S. Military Academy, West Point, NY
Robert L. Borrelli, Mathematics Dept., Harvey Mudd College, Claremont, CA

## Helix Intersections Problem

Head Judge
Marvin S. Keener, Mathematics Dept., Oklahoma State University, Stillwater, OK
Associate Judges
Ben A. Fusaro (Triage), Dept. of Mathematical Sciences, Salisbury State University, Salisbury, MD
Patrick Driscoll, Virginia Polytechnic Institute and State University, Blacksburg, VA
Mario Juncosa, RAND Corporation, Santa Monica, CA
Veena Mendiratta, AT\&T Bell Labs, Naperville, IL
Keith Miller, National Security Agency, Fort Meade, MD
Mike Moody, Harvey Mudd College, Claremont, CA

Lee Seitelman, Glastonbury, CT
Matthew Witten, University of Texas, Austin, TX
Daniel Zwillinger, Zwillinger \& Associates, Arlington, MA

## Faculty Salaries Problem

Head Judge
Maynard Thompson, Mathematics Dept., University of Indiana, Bloomington, IN
Associate Judges
Robert M. Tardiff (Triage), Dept. of Mathematical Sciences, Salisbury State University, Salisbury, MD
Karen Bolinger, Mathematics Dept., Arkansas State University, State University, AR
James Case, Baltimore, Maryland
William Fox, Dept. of Mathematical Sciences, U.S. Military Academy, West Point, NY
Jerry Griggs, University of South Carolina, Columbia, SC
Don Miller, Dept. of Mathematics, St. Mary's College, Notre Dame, IN
Peter Olsen, National Security Agency, Fort George G. Meade, MD
Judith Pastor, Haverly Systems, Inc., Houston, TX
Catherine Roberts, Mathematics Dept., University of Rhode Island, Kingston, RI
Theresa Sandifer, Mathematics Dept., Southern Connecticut State Univ., New Haven, CT
Michael Tortorella, Middletown, NJ

## Triage Session

Director
Ben A. Fusaro
Head Judge, Helix Intersections Problem
Ben A. Fusaro
Head Judge, Faculty Salaries Problem
Robert M. Tardiff
Associate Judges
Homer W. Austin
Alfred S. Beebe, University of Maryland, Eastern Shore, Princess Anne, MD
E. Boyd, University of Maryland, Eastern Shore, Princess Anne, MD

Donald C. Cathcart
S.M. Hetzler
T.O. Horseman

Peter Olsen, National Security Agency, Fort George G. Meade, MD
Fatollah Salimian
Kathleen M. Shannon
Barbara A. Wainwright
M.E. Williams
W.J. Yurek, Worcester-Wicomico Community College, Salisbury, MD

Except as noted, the triage judges were from Salisbury State University, Salisbury, MD.

## Sources of the Problems

The Helix Intersections Problem was contributed by Yves Nievergelt (Eastern Washington University, Cheney, WA), who describes its origin in his Author's Commentary in this issue. The Faculty Salaries Problem was contributed by Kathleen M. Shannon (Salisbury State University, Salisbury, MD); the data are public information from Salisbury State University.

## Acknowledgments

MCM was funded this year by the National Security Agency, whose support we deeply appreciate. We thank Dr. Gene Berg of NSA for his coordinating efforts. The MCM is also indebted to INFORMS and SIAM, which provided judges, prizes, and forums for presentations of student papers.

I thank the MCM judges and MCM Board members for their valuable and unflagging efforts. Harvey Mudd College, its Mathematics Dept. staff, and Prof. Borrelli were gracious hosts to the judges.

## Cautions

## To the reader of research journals:

Usually, a published paper has been presented to an audience, shown to colleagues, rewritten, checked by referees, revised, and edited by a journal editor. Each of the student papers here is the result of undergraduates working on a problem over a weekend; allowing substantial revision by the authors could give a false impression of accomplishment. So these papers are essentially au naturel. Light editing has taken place: minor errors have been corrected, wording has been altered for clarity or economy, and style has been adjusted to that of The UMAP Journal. Please peruse these student efforts in that context.

## To the potential MCM Advisor:

It might be overpowering to encounter such output from a weekend of work by a small team of undergraduates, but these solution papers are highly atypical. A team that prepares and participates will have an enriching learning experience, independent of what any other team does.

## Appendix: Successful Participants

KEY:
P = Successful Participation
H = Honorable Mention
$\mathrm{M}=$ Meritorious
$\mathrm{O}=$ Outstanding (published in this special issue)
A = Helix Intersections Problem
B = Faculty Salaries Problem

| INSTITUTION | CITY | ADVISOR | A | B |
| :---: | :---: | :---: | :---: | :---: |
| ALABAMA |  |  |  |  |
| Univ. of Alabama | Huntsville | Claudio H. Morales | P |  |
| ALASKA |  |  |  |  |
| University of Alaska | Anchorage | Ted L. Gifford | M |  |
|  | Fairbanks | John P. Lambert | H | O |
|  |  | Patricia A. Andresen |  | M |
| ARIZONA |  |  |  |  |
| Northern Arizona U. | Flagstaff | Terence R. Blows | P | P |
| ARKANSAS |  |  |  |  |
| Hendrix College | Conway | Ze'ev Barel |  | P |
| Williams Baptist Coll. | Walnut Ridge | Lana S. Rhoads |  | P |
|  |  | Joy Holloway |  | P |
| CALIFORNIA |  |  |  |  |
| Calif. Inst. of Tech. | Pasadena | Alexander S. Kechris | H |  |
| Calif. Poly. State Univ. | S. Luis Obispo | Thomas O'Neil Ernest Blattner | M, M | P |
| Calif. State Poly. Univ. | Pomona | James R. McKinney |  | P |
| Calif. State University | Northridge | Gholam Ali Zakeri |  | P |
| Harvey Mudd College | Claremont | David L. Bosley | O | O |
| Humboldt State Univ. | Arcata | Jeffrey B. Haag | P |  |
|  |  | Kathleen M. Crowe | H |  |
| Loyola Marymount U. | Los Angeles | Thomas M. Zachariah | P |  |
| Pomona College | Claremont | Amy Radunskaya | H |  |
| Sonoma State Univ. | Rohnert Park | Clement E. Falbo | H |  |
| Univ. of California | Berkeley | Allen M. Chen | P | H |
| Univ. of Redlands | Redlands | Alexander E. Koonce |  | P |
| COLORADO |  |  |  |  |
| Metro. State College | Denver | Thomas E. Kelley | P |  |
| Regis University | Denver | Diane M. Wagner |  | P |



| INSTITUTION | CITY | ADVISOR | A | B |
| :---: | :---: | :---: | :---: | :---: |
| KANSAS |  |  |  |  |
| Benedictine College | Atchison | Jo Ann Fellin, O.S.B. | P |  |
| KENTUCKY |  |  |  |  |
| Asbury College | Wilmore | Kenneth P. Rietz | H | H |
| Bellarmine College | Louisville | John A. Oppelt | H |  |
| Western Kentucky U. | Bowling Green | Douglas D. Mooney |  | P |
| LOUISIANA |  |  |  |  |
| McNeese State Univ. | Lake Charles | Sid L. Bradley | P |  |
|  |  | George F. Mead | P |  |
| MAINE |  |  |  |  |
| Bowdoin College | Brunswick | Adam B. Levy |  | P |
| Colby College | Waterville | Amy H. Boyd | P |  |
| University of Maine | Orono | Grattan P. Murphy | P |  |
| MARYLAND |  |  |  |  |
| Hood College | Frederick | John Boon |  | P |
| Loyola College | Baltimore | Dipa Choudhury |  | H, H |
| Mt. St. Mary's Coll. | Emmitsburg | Fred J. Portier |  | M |
|  |  | Theresa A. Francis | P |  |
| Salisbury State U. | Salisbury | Kathleen M. Shannon |  | P |
|  |  | Steve M. Hetzler | P |  |
| Univ. of Maryland | College Park | Michael C. Fu |  | P |
| MASSACHUSETTS |  |  |  |  |
| Harvard University | Cambridge | Harry R. Lewis | M, P |  |
|  |  | Roger W. Brockett | H |  |
| Smith College | Northampton | Ruth Haas |  | P |
| U. of Massachusetts | Amherst | Edward A. Connors | H | H |
| Worcester Poly. Inst. | Worcester | Arthur C. Heinricher | M |  |
|  |  | Bogdan Vernescu | H |  |
| MICHIGAN |  |  |  |  |
| Calvin College | Grand Rapids | Steven P. Dirkse | P |  |
| Eastern Michigan U. | Ypsilanti | Christopher E. Hee |  | H |
| Lawrence Tech. Univ. | Southfield | Ruth G. Favro | P |  |
|  |  | Howard Whitston | P |  |
| Southwest. Mich. C. | Dowagiac | Ronald Sawatzky |  | P |
| MINNESOTA |  |  |  |  |
| Macalester College | St. Paul | Wayne A. Roberts | O | H |
| Moorhead State Univ. | Moorhead | Ronald M. Jeppson |  | P |
| MISSISSIPPI |  |  |  |  |
| Jackson State Univ. | Jackson | David C. Bramlett | H |  |
|  |  | Carl Drake |  | P |


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| Missouri Southern St. Coll. | Joplin | Patrick Cassens |  | P,P |
| Northeast Missouri St. U. | Kirksville | Steven J. Smith |  | H |
| Northwest Missouri St. U. | Maryville | Russell N. Euler |  | P |
| Southeast Missouri St. U. | Cape Girardeau | Robert W. Sheets |  | O |
| University of Missouri | Rolla | Roger H. Hering |  | M |
| Washington University | St. Louis | Hiro Mukai | H | M |
| Wentworth Mil. Academy | Lexington | J.O. Maxwell |  | P |
| NEBRASKA |  |  |  |  |
| Hastings College | Hastings | David B. Cooke |  | H |
| Nebraska Weslyan Univ. | Lincoln | P. Gavin LaRose | P |  |
| NEVADA |  |  |  |  |
| Sierra Nevada College | Incline Village | Sue Welsch |  | P |
| NEW JERSEY |  |  |  |  |
| New Jersey Inst. of Tech. | Newark | Bruce G. Bukiet |  | P |
| NEW MEXICO |  |  |  |  |
| New Mexico State Univ. | Las Cruces | Marcus S. Cohen | H |  |
| New Mexico Tech. | Socorro | Brian T. Borchers | M |  |
| NEW YORK |  |  |  |  |
| Hofstra University | Hempstead | R.N. Greenwell | P | P |
| Ithaca College | Ithaca | John C. Maceli |  | H |
|  |  | James E. Conklin |  | H |
| Le Moyne College | Syracuse | William C. Rinaman |  | P |
| Nazareth C. of Rochester | Rochester | Ronald W. Jorgensen | H |  |
| Pace University | Pleasantville | Robert A. Cicenia |  | P |
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| Siena College | Loudonville | T.H. Rousseau | P |  |
| Westchester Comm. Coll. | Valhalla | Rowan Lindley | P |  |
| NORTH CAROLINA |  |  |  |  |
| Appalachian State Univ. | Boone | Jaimie Hebert | P |  |
|  |  | Holly Hirst | H |  |
| Duke University | Durham | David P. Kraines | M |  |
|  |  | Richard A. Scoville | H |  |
| N.C. Schl. of Sci. \& Math | Durham | Dot Doyle | H | O |
| Univ. of North Carolina | Wilmington | Russell L. Herman | ${ }^{\text {H }}$ |  |
|  | Chapel Hill | Jon W. Tolle |  |  |
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| Western Carolina Univ. | Cullowhee | Jeff A. Graham |  | P |
|  |  | Joseph S. Sportsman | H |  |


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|  | Grand Forks | David J. Uherka |  | P |
| OHIO |  |  |  |  |
| College of Wooster | Wooster | Matthew Brahm |  | P |
| Hiram College | Hiram | Michael A. Grajek James R. Case |  | P M |
| Kenyon College | Gambier | Dana N. MacKenzie | P | M |
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| Xavier University | Cincinnati | Richard J. Pulskamp | H |  |
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| Southeastern Okla. St. U. | Durant | Brett M. Elliott |  | P |
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| Southern Oregon St. C. | Ashland | Kemble R. Yates | P |  |
| PENNSYLVANIA |  |  |  |  |
| Bloomsburg University | Bloomsburg | Scott E. Inch | P |  |
| Gannon University | Erie | Rafal F. Ablamowicz | P,P |  |
| Gettysburg College | Gettysburg | James P. Fink |  | P |
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| Muhlenberg College | Allentown | David A. Nelson |  | M, P |
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| Westminster College | N. Wilmington | Carolyn Cuff |  | P |
| RHODE ISLAND |  |  |  |  |
| Rhode Island College | Providence | D.L. Abrahamson |  | P |
| SOUTH CAROLINA |  |  |  |  |
| Central Carolina Tech. C. | Sumter | Karen G. McLaurin |  | P,P |
| The Citadel | Charleston | Kanat Durgun | P |  |
| Coastal Carolina Univ. | Conway | Prashant S. Sansgiry | P |  |
| Columbia College | Columbia | Scott A. Smith |  | P |
| Francis Marion Univ. | Florence | Catherine A. Abbott |  | P |
| Midlands Tech. College | Columbia | John R. Long Rick Bailey | P | P |
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| Southwestern University | Georgetown | Therese Shelton |  | M |
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| University of Dallas | Irving | Charles A. Coppin |  | M |
| U. Texas-Pan American | Edinburg | Roger A. Knobel | P | P |
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| University of Utah | Salt Lake City | Don H. Tucker | M,P |  |
| Utah State University | Logan | Michael C. Minnotte |  | P |
| Weber State University | Ogden | Afshin Ghoreishi | P |  |
| VERMONT |  |  |  |  |
| VIRGINIA |  |  |  |  |
| Coll. of William \& Mary | Williamsburg | Lawrence M. Leemis | P | M |
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| James Madison Univ. <br> Roanoke College <br> Thomas Jefferson H. S. for Sci. \& Tech. | Harrisonburg Salem | James S. Sochacki Jeffrey L. Spielman | P |  |
|  |  |  |  | P |
|  | Alexandria | Geraldine F. Oliveto | P |  |
|  |  | Peter J. Braxton | H |  |
| University of Richmond | Richmond | Kathy W. Hoke | H |  |
| Virginia Pol. Inst. \& St. U. | Blacksburg | Joel A. Nachlas |  | H |
|  |  | Sheldon H. Jacobson | P |  |
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| Eastern Wash. Univ. | Cheney | David Jabon | P |  |
| Univ. of Puget Sound | Tacoma | Robert A. Beezer |  | P |
|  |  | Martin Jackson |  | H |
| Western Wash. Univ. | Bellingham | Tjalling J. Ypma | H | P |
| WISCONSIN |  |  |  |  |
| Alverno College | Milwaukee | Susan F. Pustejovsky |  | P, P |
| Beloit College | Beloit | Philip D. Straffin | P | P |
| Northcentral Tech. Coll. | Wausau | Frank J. Fernandes | P |  |
|  |  | Robert J. Henning | P |  |
|  |  | Carmen Olson |  | P |
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|  |  | Andrew E. Long | P |  |
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|  |  | Clement T. Jeske |  | H |
|  | Stevens Point | Norman Curet |  | H |
| BULGARIA |  |  |  |  |
| Bulgarian Acad. of Sci. | Sofia | Jordan B. Tabov | P |  |
|  |  | Petar S. Kenderov |  | H |
| CANADA |  |  |  |  |
| Scarborough College, |  |  |  |  |
| University of Calgary | Calgary, Alb. | David R. Westbrook |  | P |
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| Anhui University | Hefei | Teng Yaoqing | P |  |
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| Automation Eng'ng Coll. of Beijing Union Univ. | Beijing | Ren Kai-long |  | P |
|  |  | Wang Xin-feng | H |  |
| Beijing Institute of Tech. | Beijing | Zhao Yan-ping | M |  |
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| Beijing Normal University | Beijing | Liu Laifu | H |  |
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|  |  | Luo Shou Shan | P |  |
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|  |  | Yang Xiaoming | P | P |
| China Pharmaceutical U. | Nanjing | Yang Jing Hua | P |  |
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| Chongqing University | Chongqing | Chu Gong |  | H |
|  |  | Ren Shanqiang |  | H |
|  |  | Qu Gong | P |  |
|  |  | Liu Qiongxun |  | P |
| Dalian University of Tech. | Dalian | Yu Hong Quan |  | H |
|  |  | He Ming Feng | P |  |
| E. China U. of Sci. \& Tech. | Shanghai | Xu Sanbao |  | H, H |
|  |  | Yuanhong Lu | P, P |  |
| Fudan University | Shanghai | Cao Yuan |  | M |
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|  |  | Ye Yao-hua |  | H |
|  |  | He Ye |  | P |


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|  |  | Gao Zhenbin |  | P |
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|  | Changchun | Lin Zhenghua | H |  |
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|  |  | Gu Yudi |  | H |
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|  |  | Wu Yi | H |  |
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| U. of Sci. \& Tech. of China | Hefei | Wang Shuhe | H |  |
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|  |  | Ma Yu Xiang | M |  |
| Zhongshan University | Guangzhou | Zhang Lei | P | P |
|  |  | He Yuanjiang |  | P |
| HONG KONG |  |  |  |  |
| Hong Kong Baptist University | Kowloon | Wai Chee Shiu |  | P |
|  |  | Li Zhi Liao |  | H |
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| Trinity College Dublin | Dublin | James C. Sexton |  | M |
|  |  | Timothy G. Murphy | M |  |
| University College Galway | Galway | Patrick M. O'Leary | H |  |
|  |  | M. Tuite | M |  |
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| University of Latvia | Riga | Janis P. Vucans | P,P |  |
| LITHUANIA |  |  |  |  |
| Vilnius University | Vilnius | Algirdas Zabulionis | P |  |
|  |  | Ricardas Kudzma |  | M |
| ZIMBABWE |  |  |  |  |
| University of Zimbabwe | Harare | James Preen |  | P |

